

66. (a) The compression is “spring-like” so the maximum force relates to the distance x by Hooke’s law:

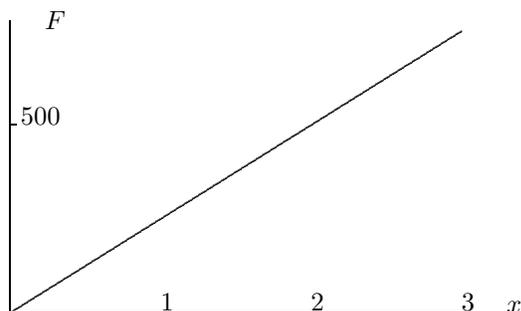
$$F_x = kx \implies x = \frac{750}{2.5 \times 10^5} = 0.0030 \text{ m} .$$

- (b) The work is what produces the “spring-like” potential energy associated with the compression. Thus, using Eq. 8-11,

$$W = \frac{1}{2} kx^2 = \frac{1}{2} (2.5 \times 10^5) (0.0030)^2 = 1.1 \text{ J} .$$

- (c) By Newton’s third law, the force

F exerted by the tooth is equal and opposite to the “spring-like” force exerted by the licorice, so the graph of F is a straight line of slope k . We plot F (in Newtons) versus x (in millimeters); both are taken as positive.



- (d) As mentioned in part (b), the spring potential energy expression is relevant. Now, whether or not we can ignore dissipative processes is a deeper question. In other words, it seems unlikely that – if the tooth at any moment were to reverse its motion – that the licorice could “spring back” to its original shape. Still, to the extent that $U = \frac{1}{2} kx^2$ applies, the graph is a parabola (not shown here) which has its vertex at the origin and is either concave upward or concave downward depending on how one wishes to define the sign of F (the connection being $F = -dU/dx$).
- (e) As a crude estimate, the area under the curve is roughly half the area of the entire plotting-area (8000 N by 12 mm). This leads to an approximate work of $\frac{1}{2}(8000)(0.012) \approx 50 \text{ J}$. Estimates in the range $40 \leq W \leq 50 \text{ J}$ are acceptable.
- (f) Certainly dissipative effects dominate this process, and we cannot assign it a meaningful potential energy.